

$$\text{FIND: } \vec{R} = \vec{F}_A + \vec{F}_B$$

$$\vec{R} = R_H \hat{i} + R_V \hat{j}$$

\therefore HORIZONTAL COMPONENTS

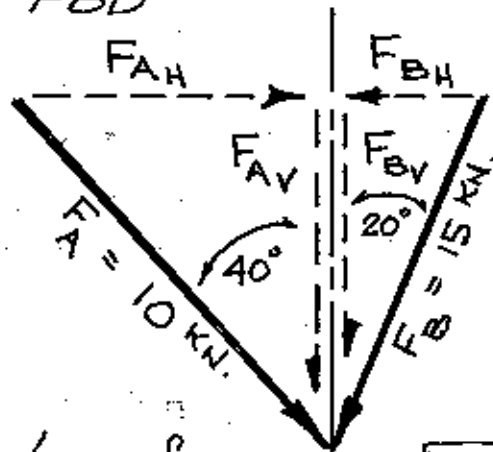
$$R_H = F_{AH} + F_{BH}$$

VERTICAL COMPONENTS

$$R_V = F_{AV} + F_{BV}$$

FOR F.B.D., EXTEND FORCE VECTORS ALONG THEIR LINE OF ACTION TO PT. O

FBD



HORIZ.

$$F_{AH} = F_A \sin 40^\circ = 10 \sin 40^\circ = 6.43 \hat{i}$$

$$F_{BH} = -F_B \sin 20^\circ = -15 \sin 20^\circ = -5.13 \hat{i}$$

$$R_H = 1.3 \hat{i}$$

VERT.

$$F_{AV} = -F_A \cos 40^\circ = -10 \cos 40^\circ = -7.66 \hat{j}$$

$$F_{BV} = -F_B \cos 20^\circ = -15 \cos 20^\circ = -14.1 \hat{j}$$

$$R_V = -21.76 \hat{j}$$

NOT TO SCALE

$$\vec{R} = 1.3 \hat{i} - 21.76 \hat{j}$$

MAGNITUDE

$$|\vec{R}| = \sqrt{(1.3)^2 + (-21.76)^2} = 21.8 \text{ KN.}$$

DIRECTION

$$\theta = \arctan \frac{R_V}{R_H} = \tan^{-1} \left[\frac{-21.76}{+1.3} \right] = -86.6^\circ$$

$$\theta = 273.4^\circ$$

$$\vec{R} = 21.8 \text{ KN. } \angle 273.4^\circ$$

POLYGON, $\vec{R} = \vec{F}_A + \vec{F}_B$ where \vec{R} is opp. $\angle 120^\circ$

LAW of COSINES

$$R^2 = F_A^2 + F_B^2 - 2(F_A)(F_B) \cos 120^\circ$$

$$R^2 = 10^2 + 15^2 - 2(10)(15) \cos 120^\circ = 475$$

$$\therefore |R| = 21.79 \text{ KN}$$

Then LAW of SINES for INTERIOR ANGLE $+50^\circ = \theta$

$$\frac{21.79}{\sin 120^\circ} = \frac{15}{\sin \alpha} \Rightarrow \alpha = 36.6^\circ + 50^\circ = 86.6^\circ = \theta$$

