

ASSUME NO FRICTION
IN THE PULLEY @ B.

P4.31
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FIND: CABLE TENSION in ABD
+ REACTION @ C

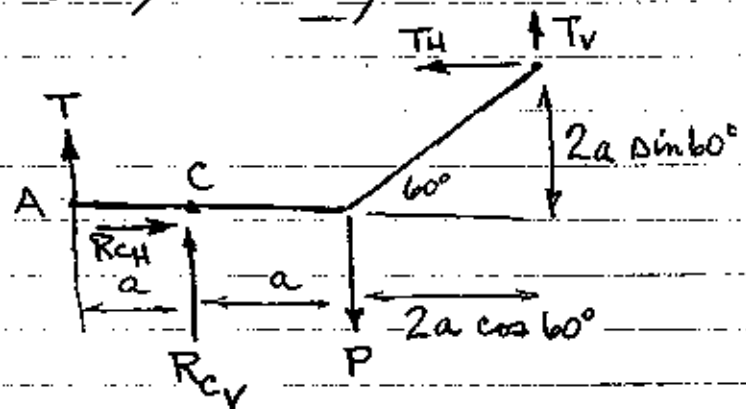
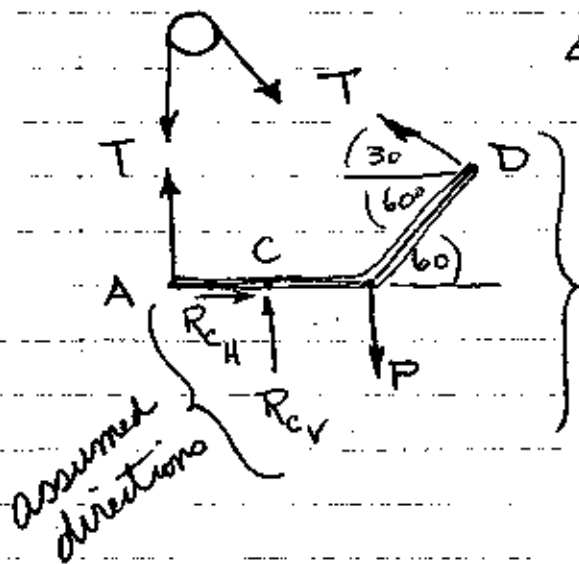
GIVEN: $\theta = 60^\circ$

SOLUTION SHOULD BE IN
TERMS OF 'P' and 'a'

FBD



SINCE THE CABLE TENSION IS
EQUAL & OPP. (or the same)
THROUGHOUT THE CABLE,
ANALYZE ONLY THE BAR.



$$\text{where } T_H = T \cos 30^\circ = .866T$$

$$T_V = T \sin 30^\circ = .5T$$

$$\sum F_x = 0 = +R_{CH} - T_H \quad \therefore \boxed{R_{CH} = .866T}$$

$$\sum F_y = 0 = +T + R_{CV} - P + T_V$$

$$\therefore R_{CV} = P - T_V - T = \boxed{P - 1.5T = R_{CV}}$$

Use pt. C as the pivot for the moments eq.

P4.31
cont'd.

$$\sum \hat{M}_C = 0 = -T a - P a + T_H (2a \sin 60^\circ) + T_V (2a \cos 60^\circ + a)$$

$$0 = -T a - P a + (.866 T)(2a \times .866) + (.5 T)(2a \times .5 + a)$$

Since all terms have an 'a', divide by 'a' to eliminate that variable.

Rewrite the eq. w/ P on one side.

$$P = -T + (.866 \times 2 \times .866) T + (.5 \times 2 \times .5 + .5) T$$
$$= -T + 1.5 T + 1.0 T$$
$$P = 1.5 T$$

$$\therefore T = 0.667 P$$

$$\text{or } \boxed{T = \frac{2}{3} P}$$

SUBSTITUTE BACK INTO FORCE EQ.

$$\text{where } R_{CH} = .866 T = .866 \left(\frac{2}{3} P \right)$$

$$\boxed{R_{CH} = 0.58 P} \rightarrow \text{assumed correct.}$$

$$\text{and } R_{CV} = P - 1.5 T = P - \frac{3}{2} \left(\frac{2}{3} P \right) = 0$$

$$\boxed{\therefore R_{CV} = 0}$$

CONCLUSION: The pin at pt. C experiences no vertical force; only the HORIZONTAL RESISTANCE.